1. Details of Module and its structure

Module Detail		
Subject Name	Physics	
Course Name	Physics 04 (Physics Part 2,Class XII)	
Module Name/Title	Unit-08, Module-02: Bohr Model	
	Chapter-12: Atoms	
Module Id	leph_201202_eContent	
Pre-requisites	Atomic structure, electrons, protons, neutrons, nucleus, Rutherford experiment as done up to secondary level, limitations of Rutherford's atomic model	
Objectives	 After going through this module the learner will be able to: Know the basic atomic structure Appreciate the role of spectrum analysis to explain atomic structure Understand the meaning of electron orbits ,energy levels, energy states and energy unit eV Interpret lowest energy -13.6 eV Deduce Velocity of electrons in different orbits Understand Bohr's model of hydrogen atom State Bohr's postulates 	
Keywords	Electron orbit, radius of orbits, velocity of electron in an orbit Bohr's postulates, -13.6 eV energy, energy levels, ground state, Bohr model	

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- **8.** Using Bohr's postulates

1. UNIT SYLLABUS

Unit 8 Atoms and Nuclei

Chapter 12 Atoms

Alpha particle scattering experiment, Rutherford's model of atom, Bohr model, energy levels, hydrogen spectrum

Chapter 13 Nuclei

Composition and size of nucleus, radioactivity, alpha, beta and gamma particles/rays and their properties, radioactive decay laws

Mass energy relations, mass defect, binding energy per nucleon and its variation with mass number, nuclear fission and nuclear fusion

2. MODULE WISE DISTRIBUTION OF UNIT SYLLABUS 7 MODULES

Introduction			
• Early models of atom			
• Alpha particle scattering and Rutherford's Nuclear model of atom			
Alpha particle trajectory			
Results and interpretations			
Size of nucleus			
What Rutherford's model could not explain			
Bohr's model of hydrogen atom			
Bohr's postulates			
Electron orbits, what do they look like?			
Radius of Bohr orbits			
 Energy levels, Energy states, energy unit eV 			
 Lowest energy -13.6 eV interpretation 			
• Velocity of electrons in orbits			

Module 3	 The line Spectrum of hydrogen atom de Broglie's explanation of Bohr 's second postulate of quantisation Departures from Bohr model energy bands Pauli's Exclusion Principle and Heisenberg's uncertainty principle leading to energy bands
Module 4	 Atomic masses and composition of nucleus discovery of neutron size of nucleus nuclear forces energy levels inside the nucleus
Module 5	 Mass and energy, Einstein's relation E = mc² Mass defect MeV Nuclear binding energy Binding energy per nucleon as a function of mass number Understanding the graph and interpretations from it
Module 6	 Radioactivity Laws of radioactivity Half life Rate of decay -disintegration constant Alpha decay Beta decay Gamma decay
Module 7	 Nuclear energy Fission Controlled fission reaction Nuclear Reactor India atomic energy programme Nuclear Fusion – energy generation in stars controlled thermonuclear fusion

MODULE 2

3. WORDS YOU MUST KNOW

Atoms: Atoms are the fundamental building blocks of matter. The existence of different kinds of matter is due to different atoms constituting them.

Molecules: A molecule is in general a group of two or more atoms that are chemically bonded together that is tightly held together by attractive forces. A molecule can be defined as the smallest particle of an element or a compound that is capable of an independent existence and

shows all the properties of that substance. Atoms of the same element or of different elements can join together to form molecules.

The molecules of an element are constituted by the same type of atoms, like hydrogen, oxygen etc

Atoms of different elements join together in definite proportions to form molecules of compounds

Charge: One of the first indications that atoms are not indivisible comes from studying static electricity .there are two kinds of charges negative and positive.

Electron: The electron is a subatomic particle, symbol e^- or β^- , whose electric charge is negative one

Proton: A *proton* is a subatomic particle, symbol p or p +, with a positive electric charge of +1e, charge on an electron and a mass slightly less than that of a neutron

Neutron: A subatomic particle of about the same mass as the proton but without an electric charge, present in all atomic nuclei except those of ordinary hydrogen.

Atomic mass:

One atomic mass unit is a mass unit equal to exactly one-twelfth (1/12th) the mass of one atom of carbon-12. The relative atomic masses of all elements have been found with respect to an atom of carbon-12

Molecular mass of a substance is the sum of the atomic masses of all the atoms in a molecule of the substance. It is therefore the relative mass of a molecule expressed in atomic mass units (u)

The mass of 1 mole of a substance is equal to its relative atomic or molecular mass in grams. The atomic mass of an element gives us the mass of one atom of that element in atomic mass units (u)

Molar mass Mass of 1 mole of a substance is called its molar mass.

Avogadro constant 6.022×10^{23} is defined as the number of atoms in exactly 12 g of carbon-12.

The mole is the amount of substance that contains the same number of particles (atoms/ ions/ molecules etc.) as there are atoms in exactly 12 g of carbon-12.or quantity of substance with a collection of 6.022×10^{23} a oms or molecules

Thomson's model of an atom Thomson proposed the model of an atom to be similar to that of a Christmas pudding. The electrons, in a sphere of positive charge, were like currants (dry fruits) in a spherical Christmas pudding.

Thomson proposed that:

- (i) An atom consists of a positively charged sphere and the electrons are embedded in it.
- (ii) The negative and positive charges are equal in magnitude. So, the atom as a whole is electrically neutral.

Rutherford's model of an atom: Ernest Rutherford was interested in knowing how the electrons are arranged within an atom. Rutherford designed an experiment for this. In this experiment, fast moving alpha (a)-particles were made to fall on a thin gold foil.

On the basis of alpha particle scattering Rutherford proposed the following model of an atom

- i) An atom consists of a small and massive central core in which the entire positive charge and almost entire mass of the atom are concentrated. The core is called the nucleus
- ii) The size of the nucleus is very small $\sim 10^{-15} m$ as compared to the size of the atom $\sim 10^{-10} m$
- iii) The nucleus is surrounded by suitable number of electrons so that the atom remains neutral
- iv) The electrons revolve around the nucleus in orbits as the planets around the sun the centripetal force is provided by the electrostatic attraction between the electrons and the nucleus

Limitations of Rutherford model of the atom

According to electromagnetic theory an accelerated charged particle must radiate electromagnetic energy. An electron revolving around the nucleus is under continuous acceleration towards the centre as they are revolving in a circle.

It should thus continuously loose energy and move in orbits with gradually decreasing radii. Finally collapse into the nucleus. BUT THE NUCLEUS is stable.

4. INTRODUCTION

Experiments carried out by Geiger and Marsden supported Rutherford's nuclear model according to this the positive charge of the atom is concentrated in a very small volume of the atom called the nucleus. The nuclear radii $\sim 10^{-15}$ m which is (1/10,000) of the atomic radius $\sim 10^{-10}$ m. The electrons in an atom remain at a relatively large distances from the nucleus, in spite of the huge electrostatic force of attraction of the nucleus for them.

Rutherford postulated that the electrons revolve about the nucleus, the force of attraction providing the requisite centripetal force to keep them in orbits.

In this module we will study the role of spectrum analysis to explain the atomic structure

5. ELECTRON ORBITS

The Rutherford nuclear model of the atom which involves classical concepts, pictures the atom as an electrically neutral sphere consisting of a very small, massive and positively charged nucleus at the centre surrounded by the revolving electrons in their respective dynamically stable orbits.

The electrostatic force of attraction, (Fe) between the revolving electrons and the nucleus provides the requisite centripetal force (Fc) to keep them in their orbits.

Thus, for a dynamically stable orbit in a hydrogen atom

$$F_e = F_C$$

$$\frac{mv^2}{r} = \frac{1}{4\pi\epsilon_0} \frac{e^2}{r^2} \quad$$

Thus the relation between the orbit radius and the electron velocity is

$$\mathbf{r} = \frac{\mathbf{e}^2}{4\pi\epsilon_0 \mathbf{m} \mathbf{v}^2} \qquad \dots \qquad 2$$

The kinetic energy (K) and electrostatic potential energy (U) of the electron in hydrogen atom are from equation 1

$$K = \frac{1}{2}mv^2 = \frac{e^2}{8\pi\varepsilon_0 r}$$

$$\mathbf{U} = -\frac{e^2}{4\pi\varepsilon_0 r} \qquad \dots \qquad 3$$

And

(The negative sign in U signifies that the electrostatic force is in the –r direction.)

Thus the total energy E of the electron in a hydrogen atom is

$$\mathbf{E} = \mathbf{K} + \mathbf{U} = \frac{\mathbf{e}^2}{8\pi\epsilon_0 \mathbf{r}} - \frac{\mathbf{e}^2}{4\pi\epsilon_0 \mathbf{r}} = -\frac{\mathbf{e}^2}{8\pi\epsilon_0 \mathbf{r}}$$

The above 4 equations give the total energy of the electron;

The energy is negative.

This implies the fact that the electron is bound to the nucleus.

It is this amount of energy that the bound electron needs to dissociate itself from the atom.

THINK ABOUT THIS

If **E** were positive, an electron will not follow a closed orbit around the nucleus and would escape the atom.

EXAMPLE

It is found experimentally that 13.6 eV energy is required to separate a hydrogen atom into a proton and an electron.

Compute the orbital radius and the velocity of the electron in a hydrogen atom.

SOLUTION

Total energy of the electron in hydrogen atom is $-13.6 \text{ eV} = -13.6 \times 1.6 \times 10^{-18} \text{ J}$

Hence from equation 4

$$E = K + U = \frac{e^2}{8\pi\varepsilon_0 r} - \frac{e^2}{4\pi\varepsilon_0 r} = -\frac{e^2}{8\pi\varepsilon_0 r}$$
$$-\frac{e^2}{8\pi\varepsilon_0 r} = -2.2 \times 10^{-18} J$$

This gives the orbital radius as-

$$r = \frac{e^2}{8\pi\epsilon_0 E} = -\frac{(9 \times 10^9 \text{Nm}^2 \text{C}^{-2})(1.6 \times 10^{=19} \text{C})^2}{(2)(-2.2 \times 10^{-18} \text{J})}$$
$$= 5.3 \times 10^{-11} m$$

The velocity of the revolving electron can be computed

Taking mass = $9.1 \times 10^{-11} kg$

$$v = \frac{e}{\sqrt{4\pi\varepsilon_0 mr}} = 2.2 \times 10^6 m/s$$

Notice the result carefully

We are saying, the radius is 5.3×10⁻¹¹ m, here order of magnitude is important

2.2×10 6 m/s is very high speed for the electrons inside the atom.

AT THAT TIME THIS WAS VERY CHALLENGING TO EXPLAIN

Spectrum of light emitted by different materials further posed a problem to think how a single electron hydrogen atom can give multiple line spectrum

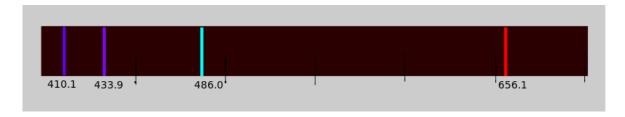
6. ATOMIC SPECTRA

It is interesting that each element emits radiation. The spectrum is a characteristic of the element or the compound, but we do not see articles around us emitting light?

When an atomic gas or vapour is excited at low pressure, usually by passing an electric current through it, the emitted radiation has a spectrum which is unique.

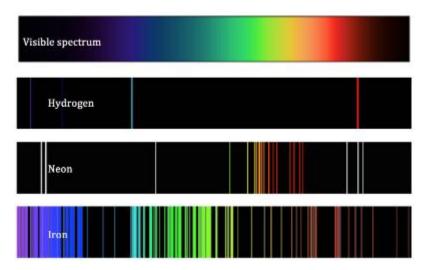
A spectrum of this kind is termed as **emission line spectrum** and it consists of bright lines on a dark background.

The spectrum emitted by atomic hydrogen is shown



https://commons.wikimedia.org/wiki/File:Bright-line_Spectrum-Hydrogen

Compare the line emission spectra of hydrogen with that of few other elements.



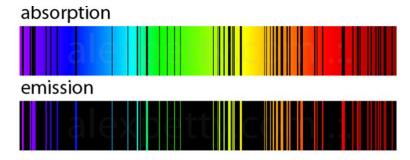
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Study of emission line spectra of a material can therefore serve as a type of "fingerprint" for identification of the element getting spectrum of any sample requires special methods. Recall the flame test you do in the chemistry laboratory for Barium, Calcium and strontium.

When white light passes through a gas and we analyse the transmitted light using a spectrometer we find some dark lines in the spectrum. These dark lines correspond precisely to those wavelengths which were found in the emission line spectrum of the gas. This is called the **absorption spectrum of the material of the gas**.

Flourine light signature

Notice the absorption apectrum is complementary to the emission spectrum .this means the light colours emitted by flourine are also the ones which are absorbed by it if a white light passes through a container filled with flourine

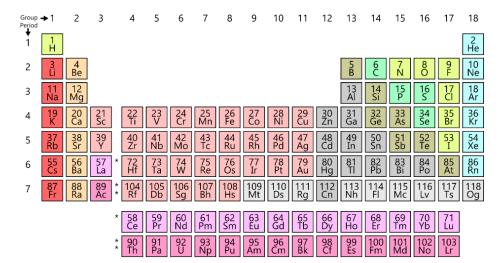


http://140.123.79.88/~a601260023/20121226HW-Reference.files/image008.png

We call it signature spectrum because each element has a characteristic spectrum, like we have signatures characteristic of individuals

We can say that, each of the elements in the periodic table have a characteristic spectrum. Some of them may give a set of very close wavelengths and the close line spectrum would then be a band spectrum

White light sources give continuous spectrum.



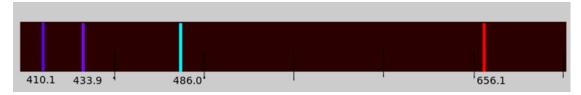
The signature spectrum is one of the ways to identify unknown elements.

SPECTRAL SERIES

We might expect that the frequencies of the light emitted by a particular element would exhibit some regular pattern.

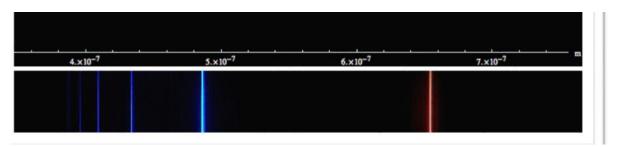
Hydrogen is the simplest atom and therefore, has the simplest spectrum.

In the observed spectrum, however, at first sight, there does not seem to be any resemblance of order or regularity in spectral lines. But the **spacing between lines within certain sets of the hydrogen spectrum decreases in a regular way.**



Each of these sets is called a spectral series.

In **1885**, the first such series was observed by a Swedish school teacher Johann Jakob Balmer (1825–1898) in the visible region of the hydrogen spectrum. This series is called **Balmer series**.



https://commons.wikimedia.org/wiki/File:BalmerFinder.GIF

Balmer found

- The line with the longest wavelength, 656.3 nm in the red is called H α ;
- The next line with wavelength 486.1 nm in the blue green is called $H\beta$,
- The third line 434.1 nm in the violet is called H γ ; and so on.
- As the wavelength decreases, the lines appear closer together and are weaker in intensity.
- Balmer found a simple **empirical formula** for the observed wavelengths.

Empirical means a result obtained by series of experiments.

$$\frac{1}{\lambda} = R\left(\frac{1}{2^2} - \frac{1}{n^2}\right)$$

Where,

 λ is the wavelength,

R is a constant called the Rydberg constant, and

n may have integral values 3, 4, 5, etc.

The value of R is 1.097×10^7 m⁻¹.

- This equation is also called Balmer formula.
 - \checkmark Taking n = 3 we can get the wavelength of the red, called Hα line

$$\frac{1}{\lambda} = R\left(\frac{1}{2^2} - \frac{1}{n^2}\right)$$
$$\frac{1}{\lambda} = 1.097 \times 10^7 \left(\frac{1}{2^2} - \frac{1}{3^2}\right)$$
$$= 1.552 \times 10^6 \text{m}^{-1}$$

i.e.,

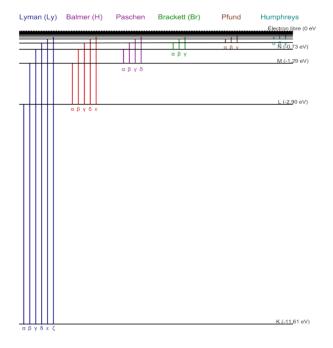
$$\lambda = 656.3 \text{ nm}$$

- \checkmark For n = 4, one obtains the wavelength of Hβ line, etc.
- ✓ For $n = \infty$, one obtains the limit of the series, at $\lambda = 364.6$ nm.

This is the shortest wavelength in the Balmer series.

Beyond this limit, no further distinct lines appear, instead only a faint continuous spectrum is seen.

Other series of spectra for hydrogen were subsequently discovered. These are known, after their discoverers, as **Lyman**, **Paschen**, **Brackett**, **and Pfund** series.



Wikipedia

The energy level diagram for the hydrogen atom, the energy with n=1 is the state of lowest energy and is called the ground state. A few of the transitions in the Lyman, Balmer, and Paschen series are also shown the separation of stationary states in (a) are not correct

These are represented by the formulae:

✓ Lyman series (Collection of wavelengths)

$$\frac{1}{\lambda} = R\left(\frac{1}{\mathbf{1}^2} - \frac{1}{n^2}\right)$$

n = 2, 3, 4...

✓ Paschen series.

$$\frac{1}{\lambda} = R\left(\frac{1}{3^2} - \frac{1}{n^2}\right)$$

n = 4, 5, 6, 7...

✓ Brackett series

$$\frac{1}{\lambda} = R\left(\frac{1}{4^2} - \frac{1}{n^2}\right)$$

n = 5, 6, 7...

✓ Pfund series

$$\frac{1}{\lambda} = R\left(\frac{1}{5^2} - \frac{1}{n^2}\right)$$

n = 6, 7, 8...

Important

The Lyman series is in ultra violet and Panchen and Brackett are in the infrared region. These lines are not visible to the eye ...this means atoms emit spectra, the distribution may or may not be visible.

• The Balmer formula may be written in **terms of frequency**

$$c = f \lambda$$

$$\frac{1}{\lambda} = \frac{f}{c}$$

$$f = Rc \left(\frac{1}{2^2} - \frac{1}{n^2}\right)$$

Important to note

There are only a few elements (hydrogen, singly ionised helium, and doubly ionised lithium) whose spectra can be represented by simple formula like given above.

The equations are useful as they give the wavelengths that hydrogen atoms radiate or absorb.

However, these results are empirical and do not give any reasoning why only certain frequencies are observed in the hydrogen spectrum.

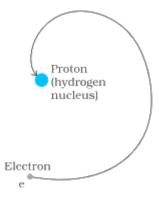
7. BOHR MODEL OF THE HYDROGEN ATOM

The model of the atom proposed by Rutherford assumes that the atom, consisting of a central nucleus and revolving electron is stable much like sun-planet system which the model imitates. However, there are some fundamental differences between the two situations. While the planetary system is held by gravitational force, the nucleus-electron system being charged objects, interact by Coulomb's Law of force.

We know that an object which moves in a circle is being constantly accelerated – the acceleration being centripetal in nature.

According to classical electromagnetic theory, an accelerating charged particle emits radiation in the form of electromagnetic waves.

The energy of an accelerating electron should therefore, continuously decrease. The electron would spiral inward and eventually fall into the nucleus



An accelerated atomic electron must spiral into the nucleus as it loses energy.

Thus, such an atom cannot be stable.

Further, according to the classical electromagnetic theory, the frequency of the electromagnetic waves emitted by the revolving electrons is equal to the frequency of revolution. As the electrons spiral inwards, their angular velocities and hence their frequencies would change continuously, and so will the frequency of the light emitted.

Thus, they would emit a continuous spectrum, in contradiction to the line spectrum observed.

Clearly Rutherford model tells only a part of the story implying that the classical ideas are not sufficient to explain the atomic structure.

EXAMPLE

According to the classical electromagnetic theory, calculate the initial frequency of the light emitted by the electron revolving around a proton in hydrogen atom.

SOLUTION

We know from the calculations that velocity (v) of electron moving around a proton in hydrogen atom in an orbit of radius (r) = 5.3×10^{-11} m is 2.2×10^{6} m/s.

Thus, the frequency of the electron moving around the proton is

$$f = \frac{v}{2\pi r}$$

$$f = \frac{2.2 \times 10^6 ms^{-1}}{2\pi (5.3 \times 10^{-11} m)}$$

$$= 6.6 \times 10^{15} \text{ Hz}$$

According to the classical electromagnetic theory we know that the frequency of the electromagnetic waves emitted by the revolving electrons is equal to the frequency of its revolution around the nucleus.

Thus the initial frequency of the light emitted is 6.6×10^{15} Hz.

But then there were so many unexplained spectral lines!!

It was Niels Bohr (1885 - 1962) who made certain modifications in this model by adding the ideas of the newly developing quantum hypothesis.

Niels Bohr studied in Rutherford's laboratory for several months in 1912 and he was convinced about the validity of Rutherford nuclear model.

Faced with the dilemma as discussed above, Bohr, in 1913, concluded that in spite of the success of electromagnetic theory in explaining large-scale phenomena, it could not be applied to the processes at the atomic scale.

It became clear that a fairly radical departure from the established principles of classical mechanics and electromagnetism would be needed to understand the structure of atoms and the relation of atomic structure to atomic spectra.

8. USING BOHR'S POSTULATES

Bohr combined **classical and early quantum concepts** and gave his theory in the form of **three postulates**.

These are:

- (i) Bohr's **first postulate** was that **an electron in an atom could revolve in certain stable orbits without the emission of radiant energy**, contrary to the predictions of electromagnetic theory. According to this postulate, each atom has certain definite stable states in which it can exist, and each possible state has definite total energy. These are called the **stationary states of the atom.**
- (ii) Bohr's **second postulate** defines these stable orbits.

This postulate states that the electron revolves around the nucleus only in those orbits for which the angular momentum is some integral multiple of $h/2\pi$

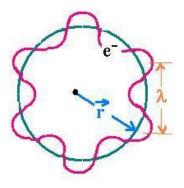
where h is the Planck's constant (= $6.6 \times 10^{-34} \text{ J s}$).

Thus the angular momentum (L) of the orbiting electron is quantised.

That is $L = nh/2\pi$

To understand this A circular orbit is taken to be stationary if its circumference contains integral number of de Broglie wavelengths.

The orbits satisfying the conditions of stationary states with 6 waves the radius of the orbit with 6 waves can be estimated



http://scientificsentence.net/Waves/images/de Broglie.jpg

(iii) Bohr's **third postulate** incorporated into atomic theory the early quantum concepts that had been developed by Planck and Einstein.

It states that an electron might make a transition from one of its specified non-radiating orbits to another of lower energy.

When it does so, a photon is emitted having energy equal to the energy difference between the initial and final states.

The frequency of the emitted photon is then given by

$$h_f = E_i - E_f$$

where E_i and E_f are the energies of the initial and final states and $E_i > E_f$.

For a hydrogen atom,

The equation

$$E = \frac{e^2}{8\pi\epsilon_0 r}$$

is sufficient to determine the energies of different energy states. But then this equation requires the radius r of the electron orbit.

Velocity of electron in an orbit

Bohr's second postulate about the angular momentum of the electron—the quantisation condition $L = n h/2\pi$ is used.

The angular momentum Lis given by L = mv r

Bohr's second postulate of quantisation says that the allowed values of angular momentum are integral multiples of $h/2\pi$.

$$L_{n} = mv_{n}r_{n} = \frac{nh}{2\pi}$$

Where n is an integer, r_n is the radius of n^{th} possible orbit and v_n is the speed of moving electron in the n^{th} orbit.

The allowed orbits are numbered 1, 2, 3 ..., according to the values of n, which is

$$v_n = \frac{e}{\sqrt{4\pi\varepsilon_0 m r_n}}$$

Using Bohr's second postulate $mv_nr_n = \frac{nh}{2\pi}$

$$v_n = \frac{1}{n} \frac{e^2}{4\pi \varepsilon_0} \frac{1}{(h/2\pi)}$$

Shows that the orbital speed in the nth falls by a factor of n

n	speed
1	$2.2 \times 10^6 \text{m/s}$
2	$\frac{1}{2}2.2 \times 10^6 = 1.1 \times 10^6 \text{ m/s}$
3	$0.73 \times 10^6 \text{ m/s}$
4	$\frac{1}{4} \times 2.2 \times 10^6 = .55 \times 10^6 \mathrm{m/s}$
	-

n	$\frac{1}{-} \times 2.2 \times 10^6 \text{m/s}$
	\mathbf{n}

We can make calculations for the magnitude of radius

$$r_n = \left(\frac{n^2}{m}\right) \left(\frac{h}{2\pi}\right)^2 \frac{4\pi\epsilon_0}{e^2}$$

For the inner most orbit n = 1

$$r_1 = \frac{h^2 \varepsilon_0}{\pi m e^2}$$

This is called the **Bohr radius** represented by the symbol **a**₀

$$a_0 = \frac{h^2 \varepsilon_0}{\pi m e^2}$$

Substitution of h ,e, m, ε_0 gives

$$a_0 = 5.29 \times 10^{-11} \text{m}$$

All other radii will be n² a₀

n	radius
1	$a_0 = 5.29 \times 10^{-11} m$
2	$\mathbf{n^2} \ \mathbf{a_0} = 4 \ \mathbf{a_0}$
3	$\mathbf{n^2} \ \mathbf{a_0} = 9 \ \mathbf{a_0}$
4	$n^2 \ a_0 = 16 \ a_0$
5	$n^2 \ a_0 = 25 \ a_0$
6	$n^2 \ a_0 = 36 \ a_0$

This shows that the separation between orbits is not the same

Energy of the electron in orbits

The total energy of the electron in the stationary states of the hydrogen atom can be obtained by the values of the corresponding radius

$$E_n = \frac{e^2}{8\pi\epsilon_0 r_n}$$

$$r_n = \left(\frac{n^2}{m}\right) \left(\frac{h}{2\pi}\right)^2 \frac{4\pi\epsilon_0}{e^2}$$

$$E_n = -\left(\frac{e^2}{8\pi\epsilon_0}\right) \left(\frac{m}{n^2}\right) \left(\frac{2\pi}{h}\right)^2 \left(\frac{e^2}{4\pi\epsilon_0}\right)$$

$$or \quad E_n = -\frac{me^4}{8n^2\epsilon_0^2 h^2}$$

$$= -13.6 \text{ eV/n}^2$$

Substituting the values in the equation

We get

$$E_n = -\frac{2.18 \times 10^{-18}}{n^2} J$$

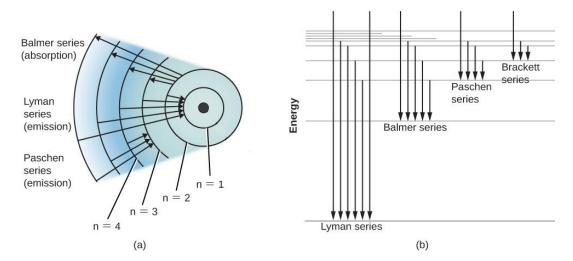
Atomic energies are often expressed in eV (electron volt) rather than in joules

$$1 \text{ e V} = 1.6 \times 10^{-19} \text{ J}$$

n is called the principle quantum number.

The **negative sign of the total energy** of an electron moving in an orbit means that the **electron is bound with the nucleus**.

Energy will thus be required to remove the electron from the hydrogen atom to a distance infinitely far away from its nucleus (or proton in hydrogen atom).



https://upload.wikimedia.org/wikipedia/commons/b/b0/Energy-Level Diagrams for Hydrogen.png

The energy level diagram for the hydrogen atom, the energy with n = 1 is the state of lowest energy and is called the ground state. A few of the transitions in the Lyman, Balmer, and Paschen series are also shown. The separation of stationary states in (a) are not correct

TRY THESE

- What is the shortest wavelength present in the Paschen series of spectral lines?
- A difference of 2.3 eV separates two energy levels in an atom. What is the frequency of radiation emitted when the atom makes a transition from the upper level to the lower level?
- The ground state energy of hydrogen atom is -13.6 eV. What are the kinetic and potential energies of the electron in this state?
- A hydrogen atom initially in the ground level absorbs a photon, which excites it to the n = 4 level. Determine the wavelength and frequency of photon.
- Using the Bohr's model calculate the speed of the electron in a hydrogen atom in the n = 1, 2, and 3 levels. (b) Calculate the orbital period in each of these levels.
- The radius of the innermost electron orbit of a hydrogen atom is 5.3×10^{-11} m. What are the radii of the n = 2 and n = 3 orbits?
- A 12.5 eV electron beam is used to bombard gaseous hydrogen at room temperature. What series of wavelengths will be emitted?

THINK ABOUT THIS

- (a) The force between electron and proton is mutually attractive. we consider electron to move around the proton. Why?
- (b) Proton mass is 2000 times the mass of electron so the lighter particles revolves around the heavier one
- (c) The force of attraction between Electron and proton follows inverse square law. the motion under such forces follows elliptical path. Then why are we choosing circular orbits, why?
- (d) Circular orbit around the nucleus were assumed. With quantum mechanics this assumption is not required.

9. SUMMARY

In this module we have learnt

- All elements give signature spectrum
- The spectrum is obtained by placing the element in suitable condition
- Hydrogen spectrum had distinct lines in red bluish green and violet regions of the visible spectrum
- Rutherford's model could not explain hydrogen spectrum
- Bohr assumed stationary orbits for electrons .these are energy possibilities where an electron can move without radiating.
- Bohr proposed three postulates
 - i) Bohr's first postulate an electron in an atom could revolve in certain stable orbits without the emission of radiant energy, these are called the stationary states of the atom.
 - ii) Bohr's **second postulate** defines these stable orbits.

This postulate states that the electron revolves around the nucleus only in those orbits for which the angular momentum is some integral multiple of $h/2\pi$

Where h is the Planck's constant (= 6.6×10^{-34} J s).

Thus the angular momentum (L) of the orbiting electron is quantised.

That is $L = nh/2\pi$

iii) It states that an electron might make a transition from one of its specified non-radiating orbits to another of lower energy

- The possible circular orbits are not equally spaced if the radius of 1 orbit given by $n = 1 = a_0$ n=2 orbit has a radius of 4 a_0
- The energy in the lowest state is -13.6 e V the energy in higher states n=2,3,4... is more